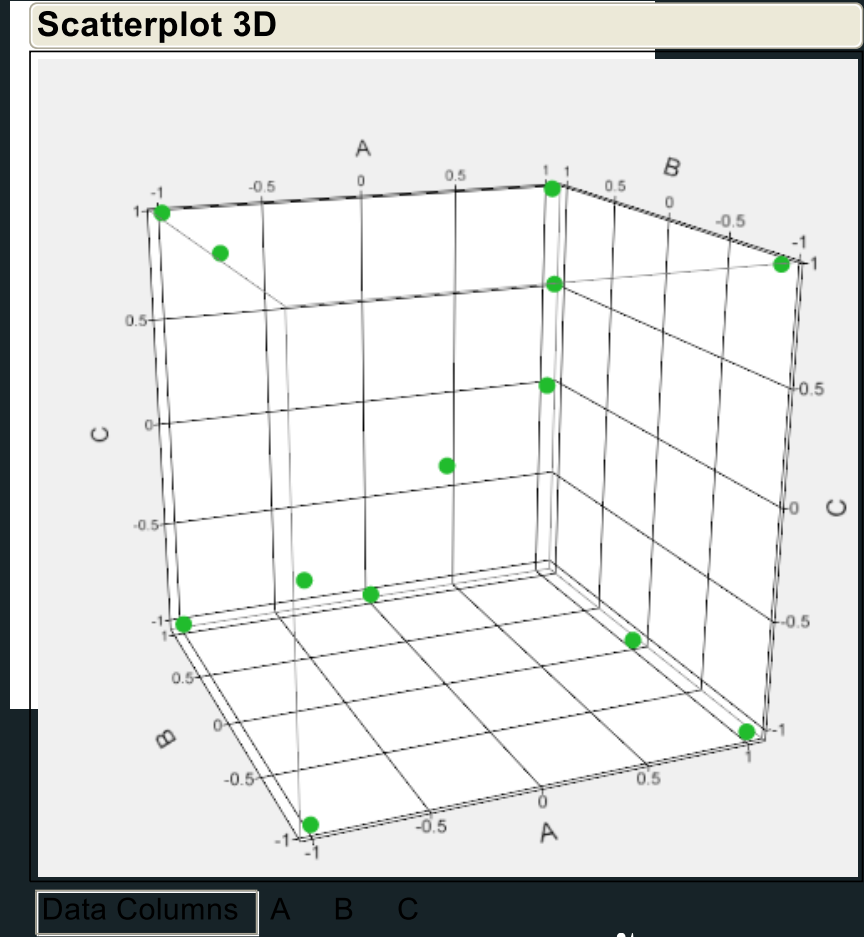
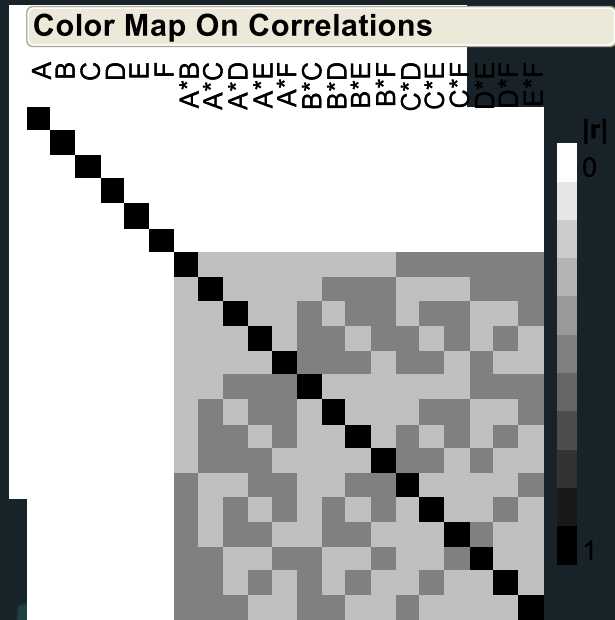
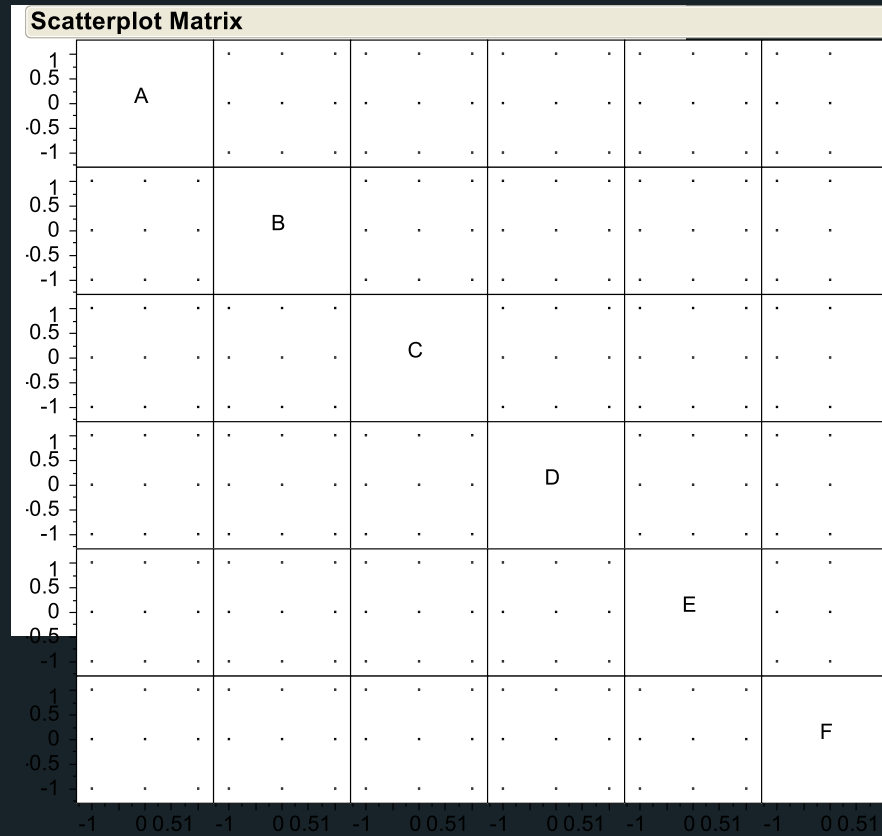


Definitive Screening Design (DSD)

Attractive alternative to Classic 2-level screening designs

	A	B	C	D	E	F
1	0	1	-1	-1	-1	-1
2	0	-1	1	1	1	1
3	1	0	-1	1	1	-1
4	-1	0	1	-1	-1	1
5	-1	-1	0	1	-1	-1
6	1	1	0	-1	1	1
7	-1	1	1	0	1	-1
8	1	-1	-1	0	-1	1
9	1	-1	1	-1	0	-1
10	-1	1	-1	1	0	1
11	1	1	1	1	-1	0
12	-1	-1	-1	-1	1	0
13	0	0	0	0	0	0



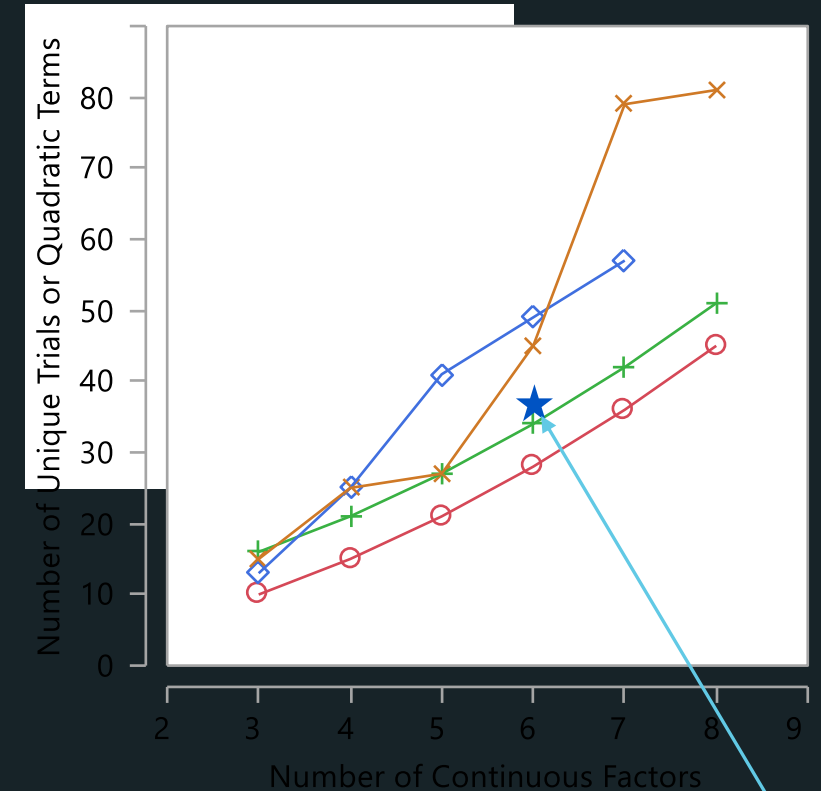
Augmentation via Custom DOE

IF MORE THAN A FEW FACTORS ARE SIGNIFICANT FOR DSD,
THEN AUGMENT DESIGN TO SUPPORT 2ND ORDER MODEL

	A	B	C	D	F	G	Block	Yield @ Time t
14	0	0	0	0	0	0	1	7.49
15	1	1	-1	1	-1	1	1	0.98
16	1	1	1	-1	-1	0	1	0.86
17	-1	1	-1	-1	1	1	1	1.25
18	1	-1	1	1	-1	-1	1	1.03
19	1	1	0	-1	1	-1	1	1.07
20	0	0	0	0	0	0	1	7.33
21	1	-1	-1	0	1	-1	1	2.61
22	-1	-1	0	1	-1	1	1	11.39
23	-1	0	1	-1	1	1	1	12.96
24	1	1	-1	1	1	1	1	1.18
25	1	0	1	1	-1	1	2	•
26	1	-1	0	1	1	0	2	•
27	1	-1	-1	1	0	1	2	•
28	1	-1	0	-1	0	-1	2	•
29	1	0	-1	-1	1	0	2	•
30	1	1	0	-1	0	1	2	•
31	1	0	1	0	1	-1	2	•
32	-1	-1	0	0	1	1	2	•
33	0	0	1	1	-1	-1	2	•
34	-1	-1	1	0	0	0	2	•
35	0	1	1	0	1	0	2	•
36	0	1	-1	1	1	-1	2	•

NOTE: First 13 rows
of original design
are not shown.

These 12 trials added onto
original 24 trials to support
full quadratic model in 6
most important factors plus a
block effect between original
and augmented trials



36 trial I-optimal response-surface design started
as 10-factor DSD and was then augmented with
12 more trials in 6 most important factors

3-Component Mixture DOE with constraints

RARELY DO COMPONENTS RANGE FROM 0 TO 1,
UNLESS TAKING UP THE SLACK IN A BLEND, LIKE WATER.
VERY OFTEN ADDITIONAL CONSTRAINTS

Study mixture components in a DOE use ranges that are proportions:

- O: 0.500 to 0.750 ($\frac{1}{2}$ to $\frac{3}{4}$)
- W: 0.000 to 0.250 (0 to $\frac{1}{4}$)
- V: 0.125 to 0.375 ($\frac{1}{8}$ to $\frac{3}{8}$)

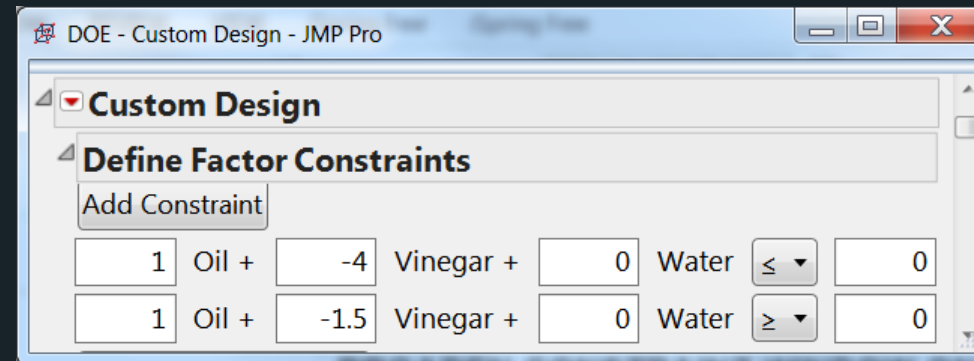
Sum of proportions *constrained* to equal 1.

$1 = O + W + V$ so therefore...

$$W = 1 - (O + V),$$

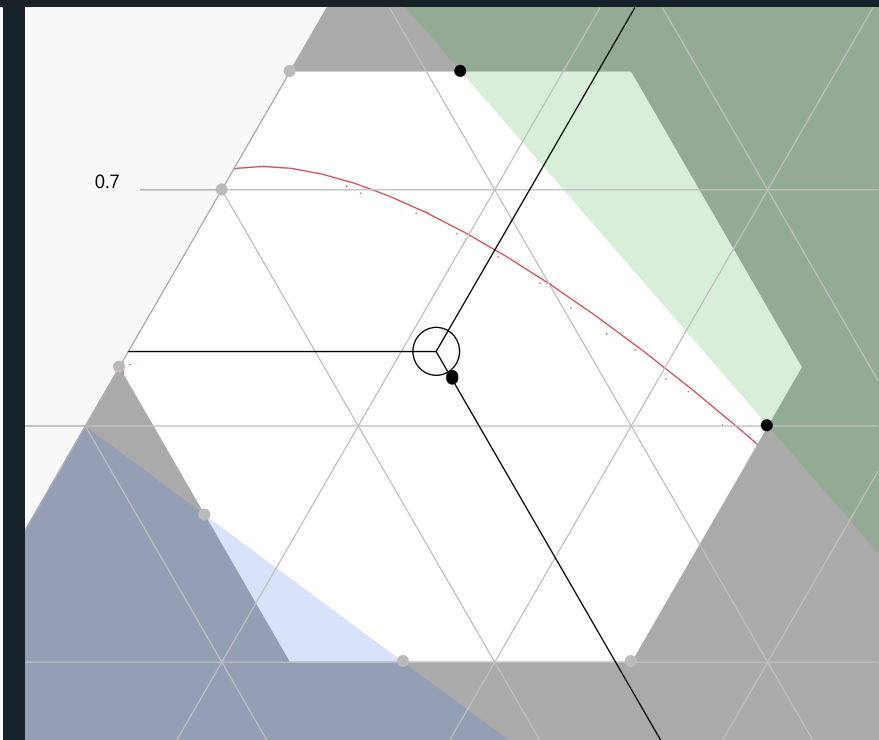
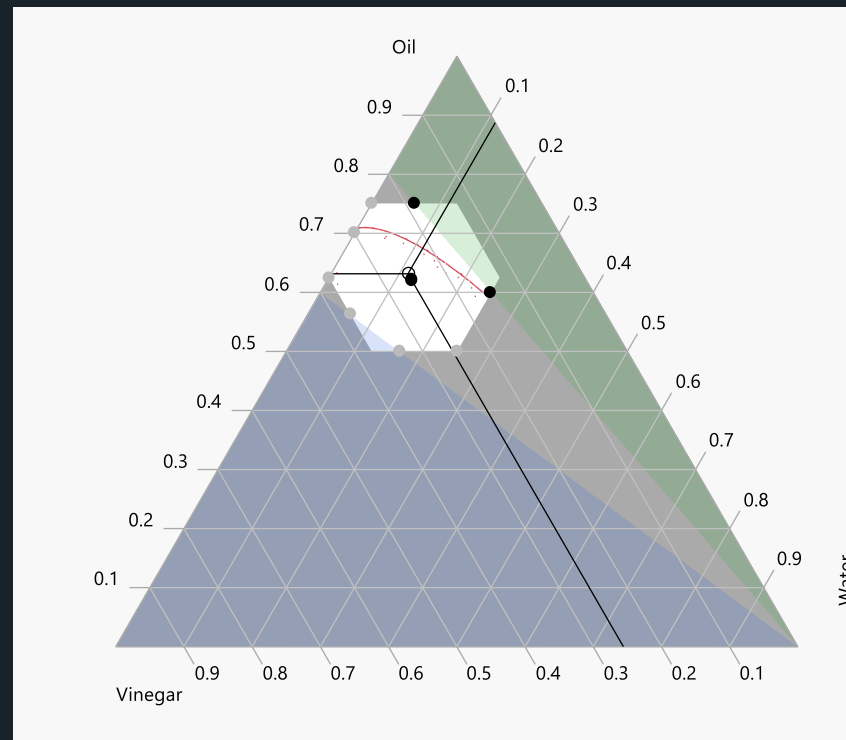
$$O = 1 - (V + W), \text{ \&}$$

$$V = 1 - (O + W)$$



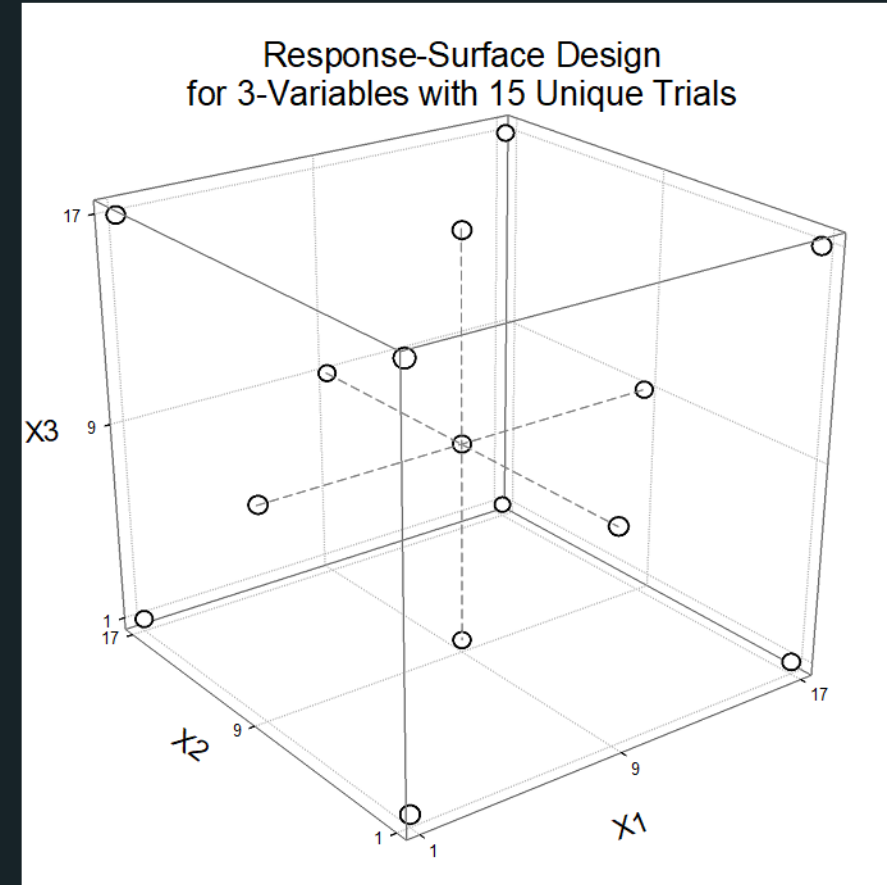
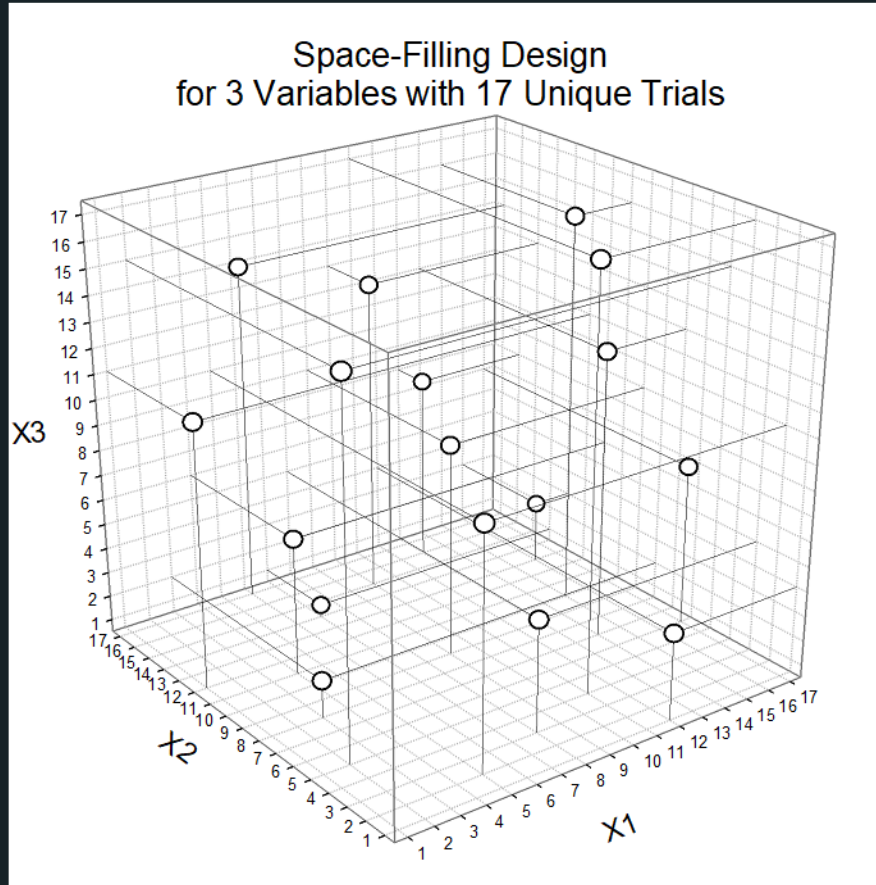
Ratio of Oil/Vinegar Constrained

$$1.5 \leq O/V \leq 4$$



Space-filling DOE for Simulations

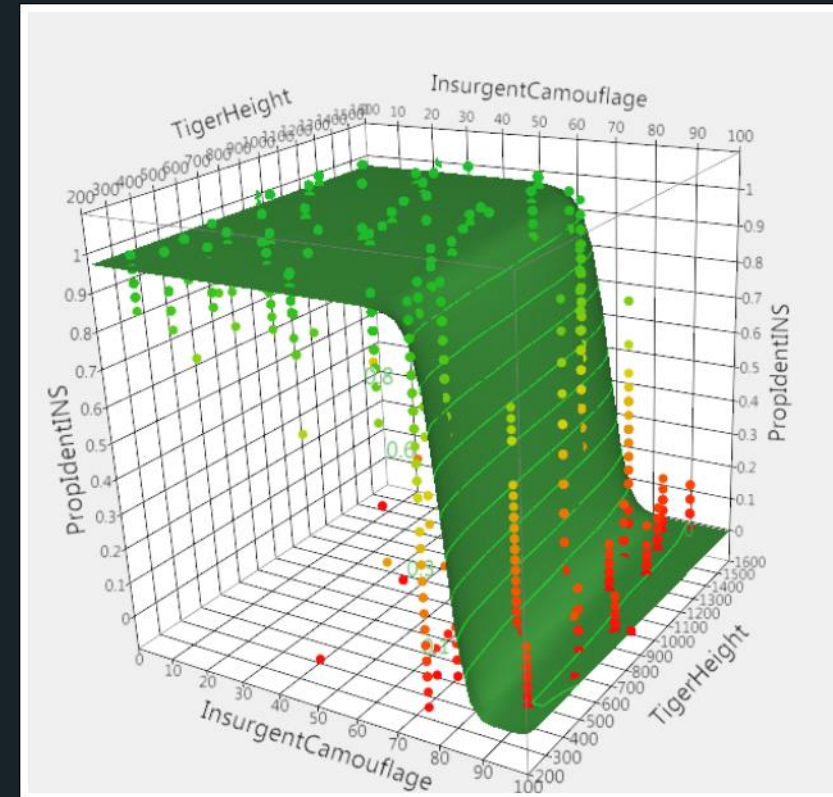
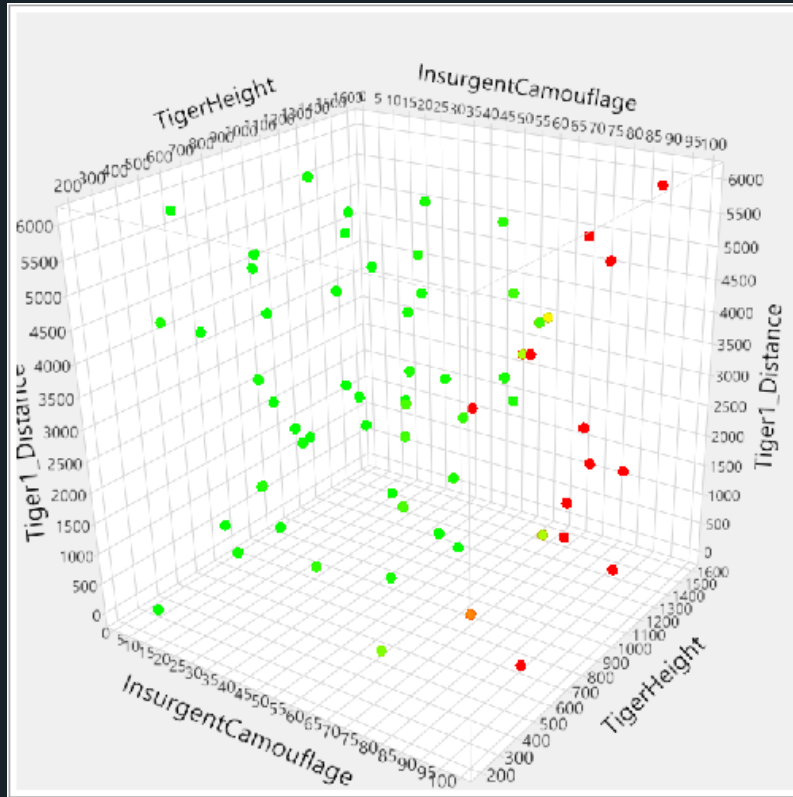
HOW ARE SPACE-FILLING DESIGNS DIFFERENT FROM TRADITIONAL DOE?



Rather than emphasizing high leverage trials (“corners”) for a simple polynomial model, space-filling designs “spread” their trials more uniformly through the space to better capture the local complexities of the simulation model.

Space-filling DOE for Simulations

SPACE-FILLING DESIGNS ARE BETTER ABLE TO DETECT WHEN A PROCESS FALLS OFF A CLIFF OR HAS A SPIKE

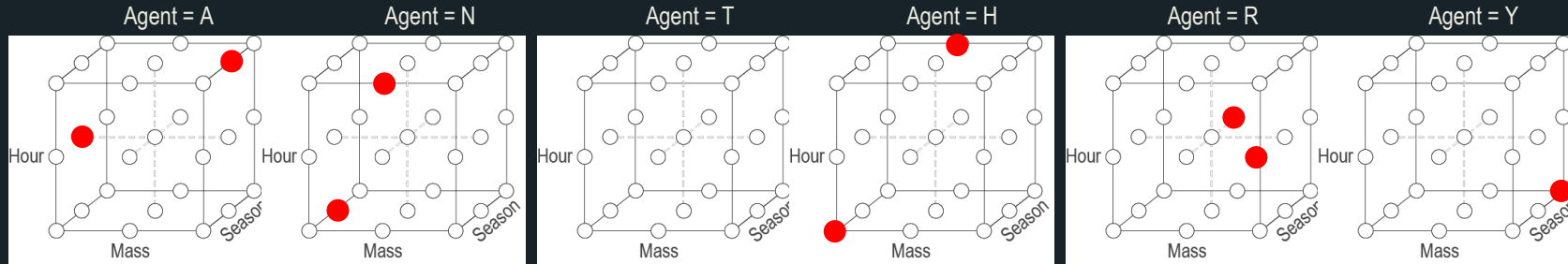


Rather than emphasizing high leverage trials (“corners”) for a simple polynomial model, space-filling designs “spread” their trials more uniformly through the space to better capture the local complexities of the simulation model.

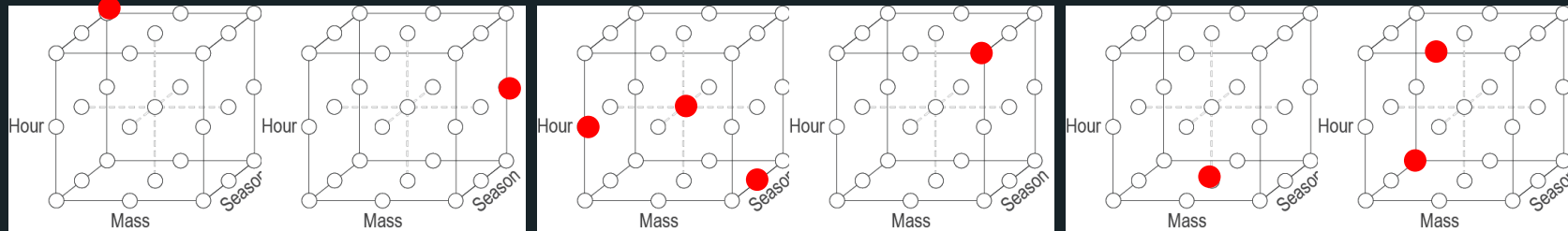
Sequential Experimentation

36 OF ALL 648 POSSIBLE COMBINATIONS OF SETTINGS
FOR 6 VARIABLES (6 X 2 X 2 X 3 X 3 X 3)

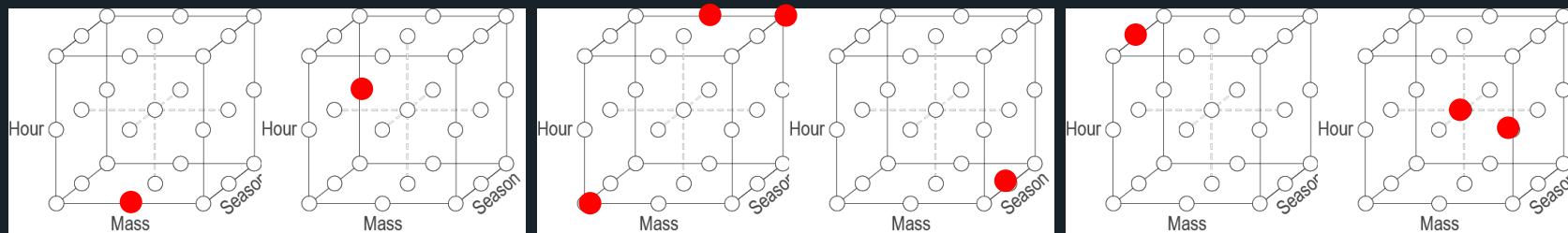
TBM = 1,
HoB = 0



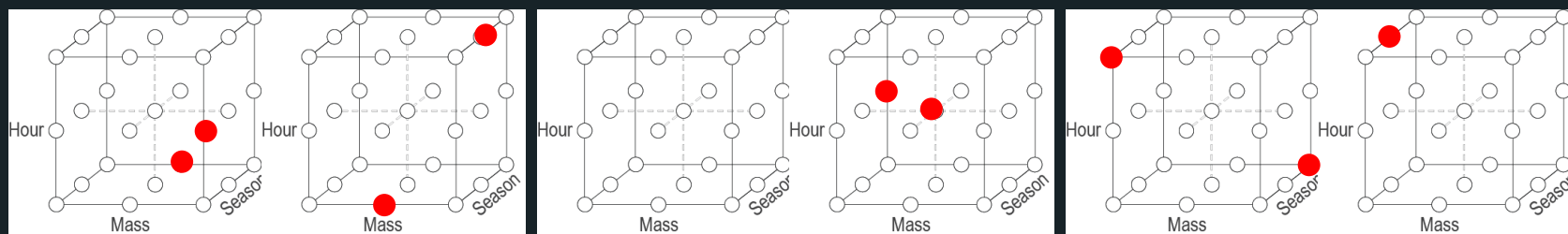
TBM = 2,
HoB = 10



TBM = 1,
HoB = 0



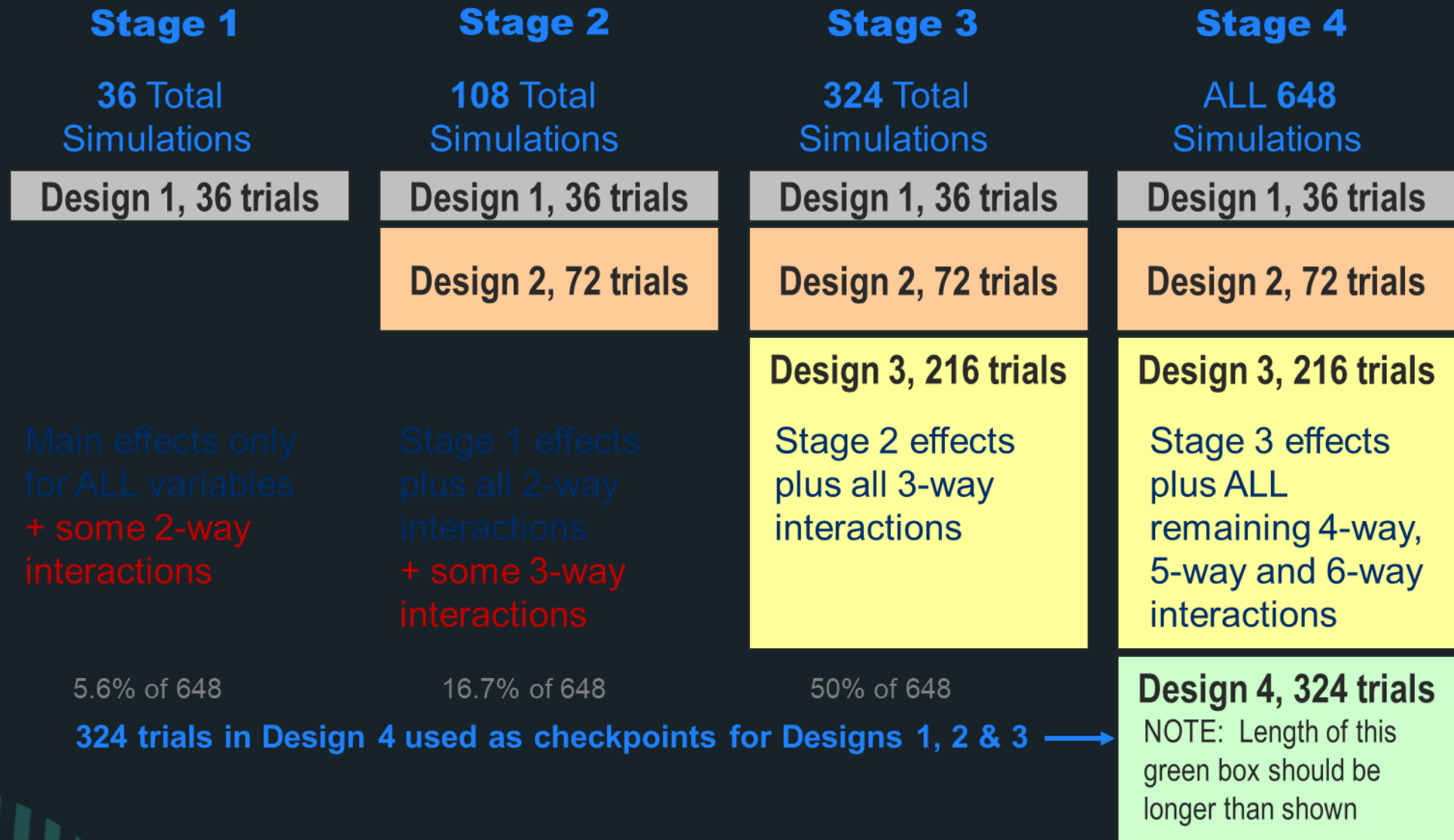
TBM = 2,
Hob = 10



Red Dots Mark the 36 Trials (an Orthogonal Array) Analyzed for Stage 1

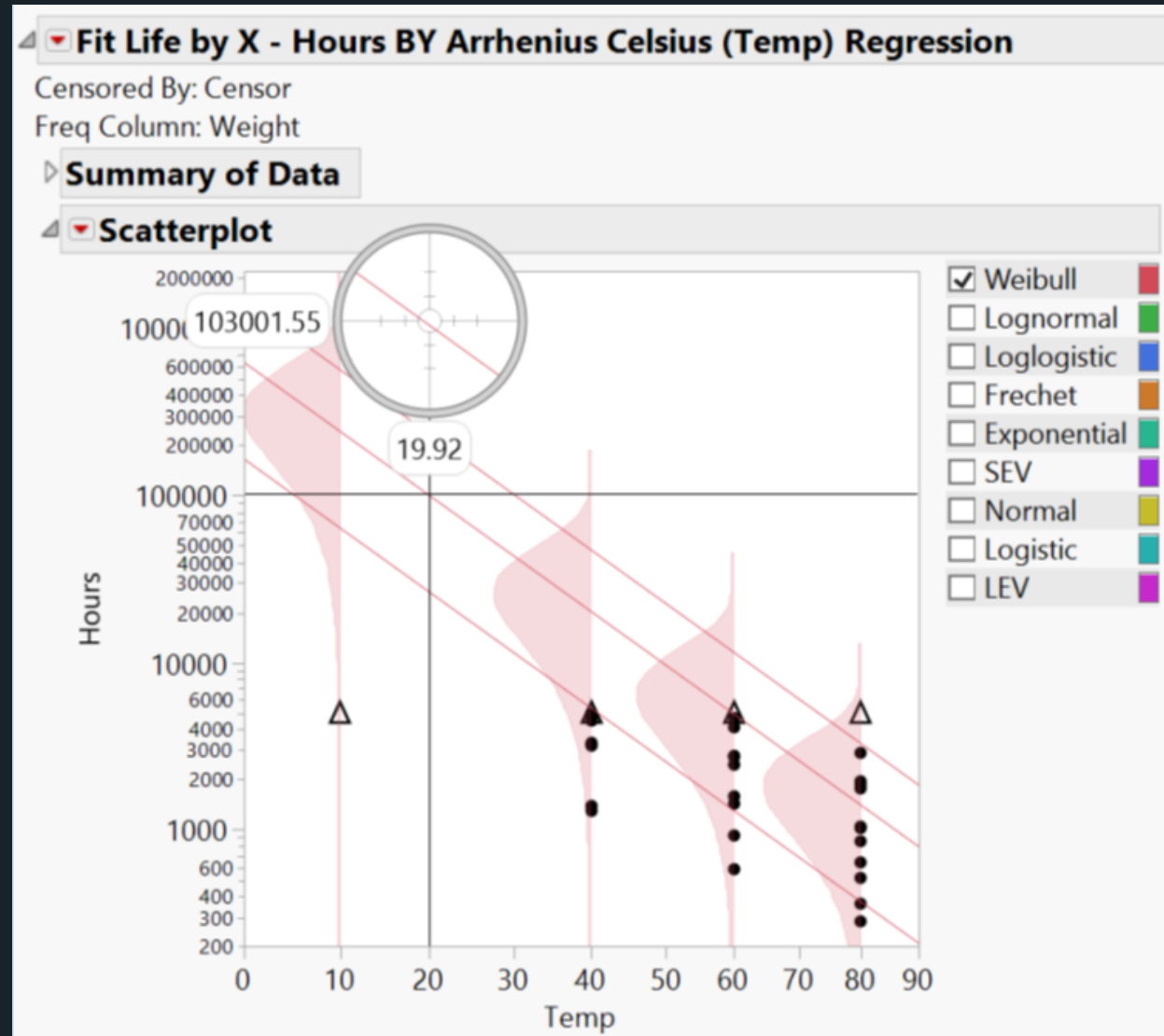
Sequential Experimentation

FOUR STAGE DESIGN SUPPORTING INCREASING COMPLEXITY OF MODEL



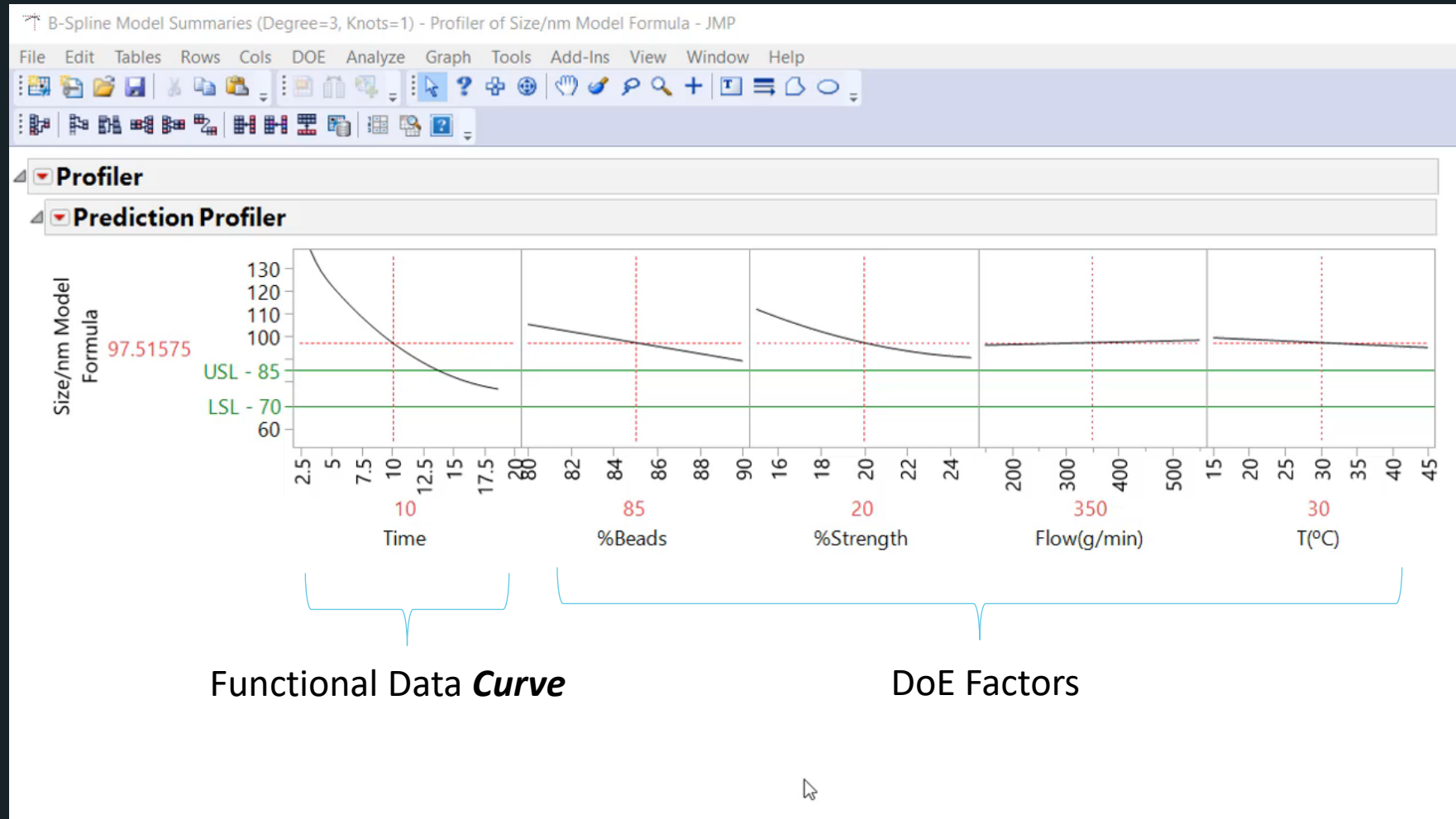
Accelerated Life Test Design

TAKE TRIALS WHERE THEY GIVE THE BEST INFORMATION

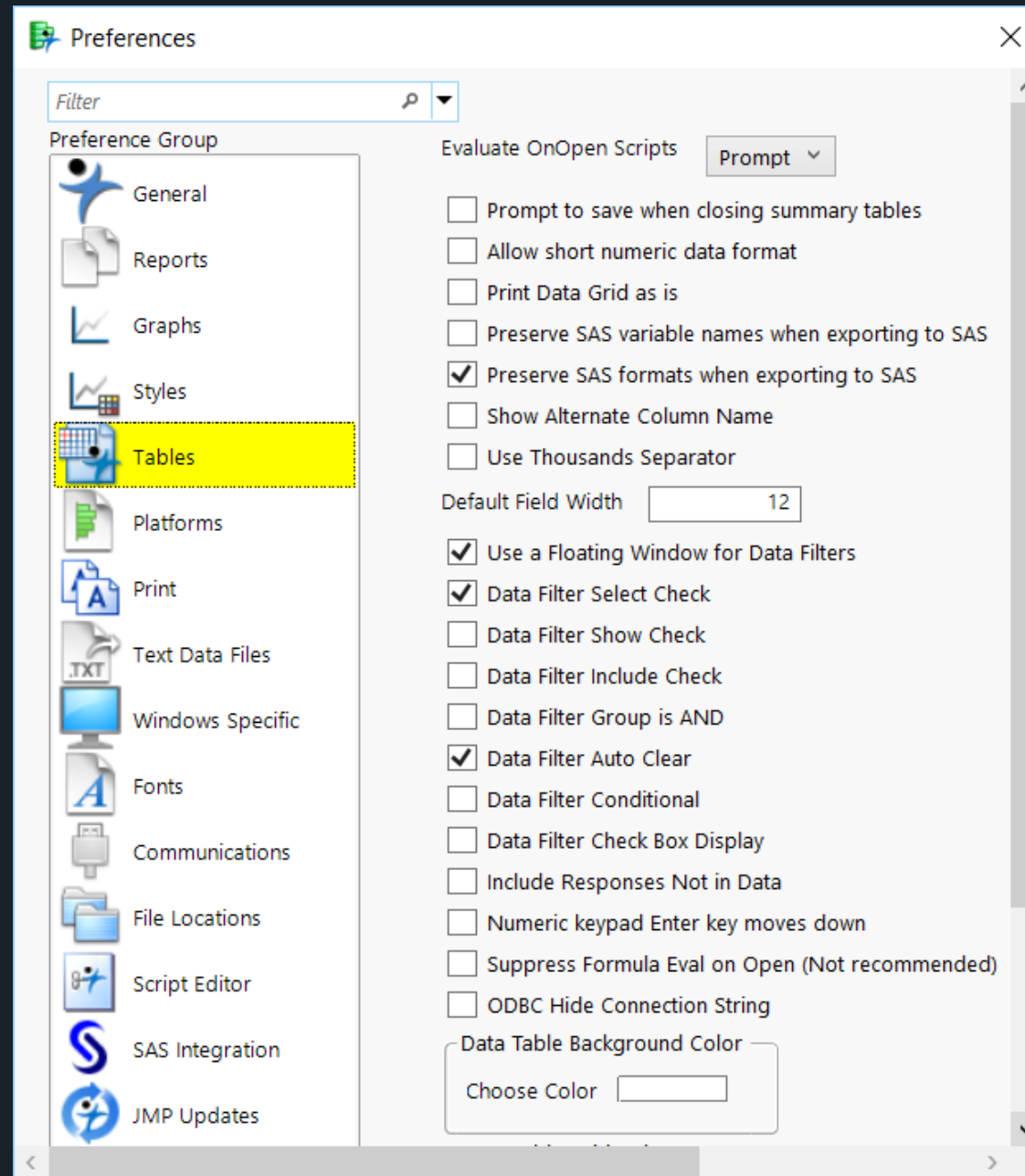


Functional Data Analysis for DOE

MODELING THE "SHAPE" OF A STREAM OF DATA – SHAPE IS THE FUNDAMENTAL UNIT OF OBSERVATION – DIMENSION REDUCTION WITH FUNCTIONAL PCA



Covering Arrays Fewest Tests for N-way Coverage



Twenty check boxes in
this dialog box

$2^{20} = 1,048,576$
possible combinations

How many tests to
check:

All pairs?

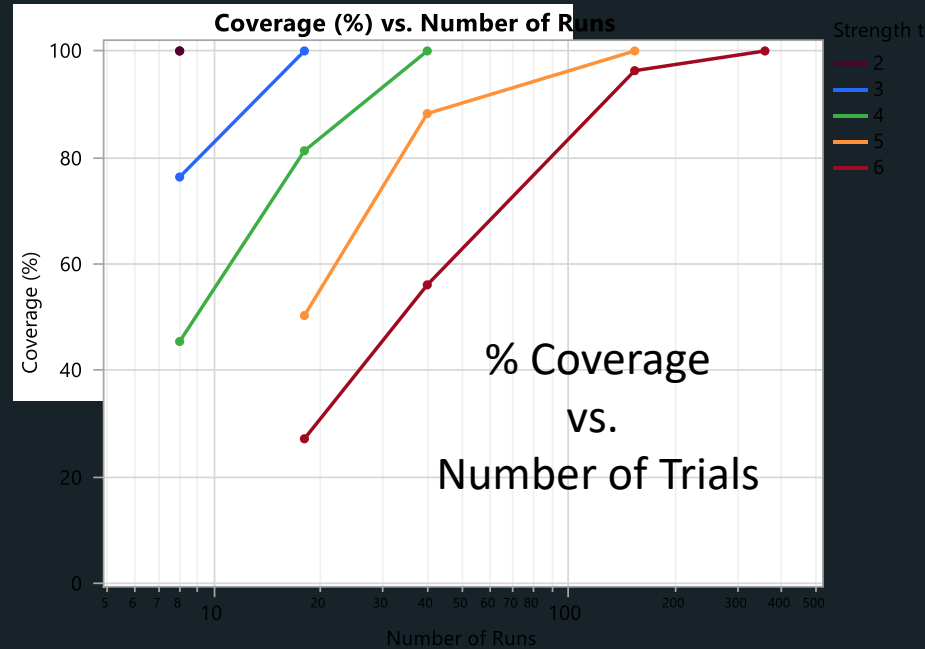
All triples?

All quadruples?

All quintuples?

All sextuples?

Covering Arrays Fewest Tests for N-way Coverage



Number of Runs: 8

t	Coverage	Diversity
2	100.00	50.00
3	76.32	76.32
4	45.43	90.87

Number of Runs: 18

t	Coverage	Diversity
3	100.00	44.44
4	81.25	72.22
5	50.30	89.42
6	27.16	96.57

Number of Runs: 40

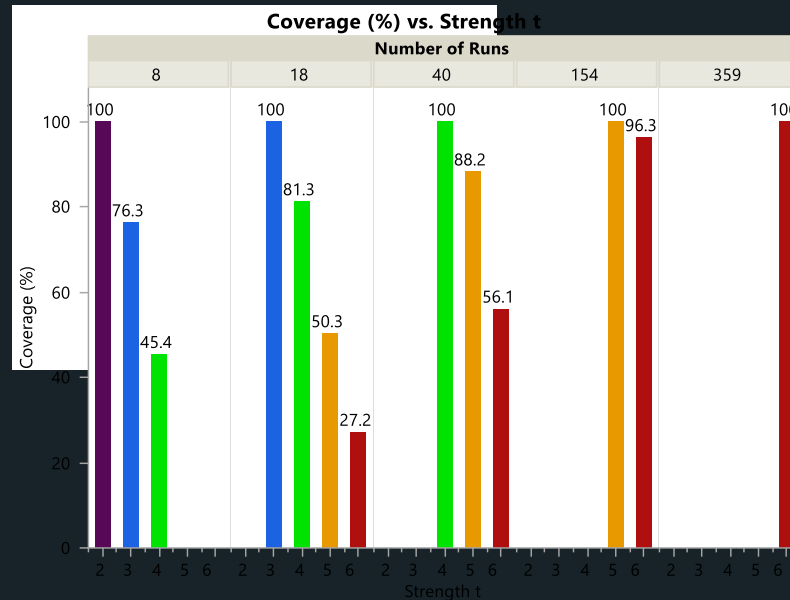
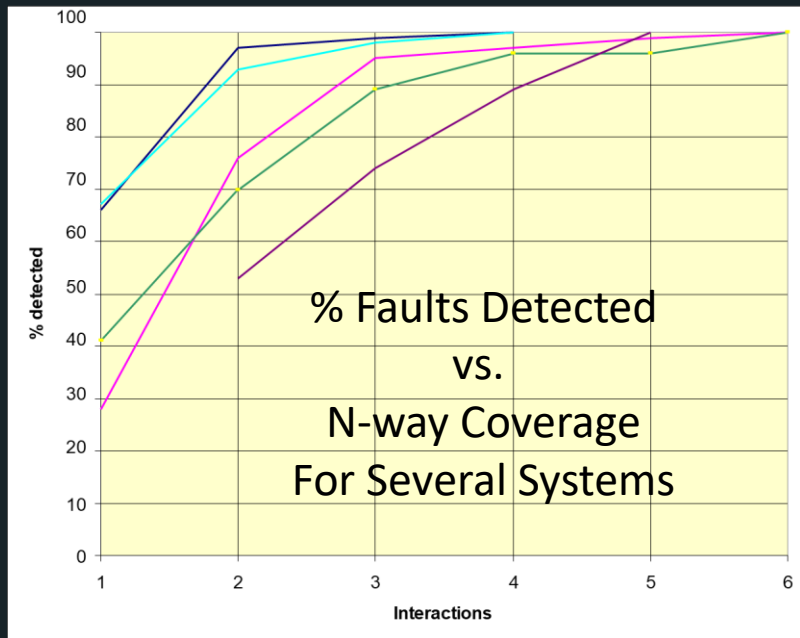
t	Coverage	Diversity
4	100.00	40.00
5	88.24	70.59
6	56.07	89.71

Number of Runs: 154

t	Coverage	Diversity
5	100.00	20.78
6	96.39	40.06

Number of Runs: 359

t	Coverage	Diversity
6	100.00	17.83



Graph courtesy of Rick Kuhn, NIST