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A (Very) Brief Intro to DOE





• It's not







• And it's not



- Design of Experiments
 - But wait! Aren't *all* experiments "designed"?!?
 - Well, not all...
 - ...are designed with the end analysis in mind, and...
 - Not all meet the primary requirement of a DOE

What is that primary requirement?

- The ability to vary all the important input parameters to the desired levels
 - Many types of experiments do not allow you to set the inputs, rather, you can only observe the inputs

So, what is DOE?

- "...the process of planning the experiment so that the appropriate data that can be analyzed by statistical methods will be collected, resulting in valid and objective conclusions."
 - Douglas Montgomery, Design and Analysis of Experiments, 5th ed, pg 11



- "...a planned approach for determining cause and effect relationships."
 - Mark Anderson & Patrick Whitcomb, DOE Simplified, pg ix

- "...consists of purposeful changes of the inputs (factors) to a process in order to observe the corresponding changes in the outputs (responses)."
 - Stephen Schmidt and Robert Launsby, *Understanding Industrial Designed Experiments*, 3rd ed, pg 1-2

- "The generation of response data from systematically selected combinations of input factors that are used to create mathematical models (equations) from which valid and objective conclusions about the inputs and outputs can be inferred."
 - Steve Figard, *Biostatistics with JMP-An Introductory Course*, in process



Goals of DOE

- To identify (screening)
- To predict (RSM)
 - "Prediction is very hard, especially when it is about the future."
 - Yogi Berra
- To do so with minimum resources



Why DOE?

- Best to explain by way of contrast to OFAT
 - <u>Not</u> how you respond to your significant other's question about how her new dress makes her look!
- <u>One-factor-a</u>t-a-<u>t</u>ime: the time honored, traditional way of doing experiments via the scientific method



Why DOE?

- What's wrong with OFAT...?
 - Can miss the true optimum
 - Does not account for interactions
 - Has lower statistical power of analysis













DOE in JMP



Design Selection?

• Determining what combinations of factors to run





• Creating the equation that connects the input variable(s) to the response variable

- Linear model in 1 variable
 - \circ y = a + bx
 - slope in x direction
 - i.e., slope in X,Y plane
 - no slope in z direction
 - line for z = 0





- Plane: Linear Model in 2 Variables
 - y = a + bx + cz
 - Used to analyze screening designs
 - No curvature
 - No interactions
 - x and z are "Main Effects"



• Interaction Twists Plane

- \circ y = a + bx + cz + dxz
- Still no curvature
- xz is an interaction between x and z





• Curvature in x Variable Only

• $y = a + bx + cz + dxz + ex^2$





- Quadratic Allows Curves In All Variables
 - $\circ \mathbf{y} = \mathbf{a} + \mathbf{b}\mathbf{x} + \mathbf{c}\mathbf{z} + \mathbf{d}\mathbf{x}\mathbf{z} + \mathbf{e}\mathbf{x}^2 + \mathbf{f}\mathbf{z}^2$
 - Used to analyze standard response surface designs
 - Constitutes the overwhelming majority of cases in "Nature"

Quadratic Model



• Partial Cubic Allows Curves Both Up and Down in All Variables

 $\circ \mathbf{y} = \mathbf{a} + \mathbf{b}\mathbf{x} + \mathbf{c}\mathbf{z} + \mathbf{d}\mathbf{x}\mathbf{z} + \mathbf{e}\mathbf{x}^2 + \mathbf{f}\mathbf{z}^2 + \mathbf{g}\mathbf{x}^2\mathbf{z} + \mathbf{h}\mathbf{x}\mathbf{z}^2$

Partial Cubic Model



Practice DOE

- Hand-Eye Coordination
 - Two factors
 - Hand: Dominant vs. Non-dominant
 - Target Diameter: small vs. large
 - Response
 - The number of dots the "operator" can mark
 - in two circles
 - alternating between circles
 - in 10 seconds
 - subtracting one from your count for each dot outside either circle

Practice DOE

- For *efficient* data collection, we need...
 - Three (3) volunteers
 - Operator to make the dots
 - Timer to time the 10 seconds
 - Someone to count the dots while data collection continues
- But let's go to JMP to set up the experiment while you cogitate on which you want to volunteer to do...